### 0.1 Star Delta Transformation



Figure 1

$$
\begin{align*}
& R_{x}+R_{y}=\frac{R_{x y}\left(R_{y z}+R_{z x}\right)}{R_{x y}+R_{y z}+R_{z x}}  \tag{1}\\
& R_{y}+R_{z}=\frac{R_{y z}\left(R_{z x}+R_{x y}\right)}{R_{x y}+R_{y z}+R_{z x}}  \tag{2}\\
& R_{z}+R_{x}=\frac{R_{z x}\left(R_{x y}+R_{y z}\right)}{R_{x y}+R_{y z}+R_{z x}} \tag{3}
\end{align*}
$$

Equation (1)-(2)

$$
\begin{equation*}
R_{x}-R_{z}=\frac{R_{x y} R_{z x}-R_{y z} R_{z x}}{R_{x y}+R_{y z}+R_{z x}} \tag{4}
\end{equation*}
$$

Equation (3)+(4)

$$
\begin{align*}
2 R_{x} & =\frac{2 R_{x y} R_{z x}}{R_{x y}+R_{y z}+R_{z x}} \\
R_{x} & =\frac{R_{x y} R_{x z}}{R_{x y}+R_{y z}+R_{z x}} \tag{5}
\end{align*}
$$

Similarly

$$
\begin{align*}
& R_{y}=\frac{R_{y z} R_{y x}}{R_{x y}+R_{y z}+R_{z x}}  \tag{6}\\
& R_{z}=\frac{R_{z y} R_{z x}}{R_{x y}+R_{y z}+R_{z x}} \tag{7}
\end{align*}
$$

## Star to Delta Transformation

$$
\begin{aligned}
& R_{x} R_{y}=\frac{R^{2}{ }_{x y} R_{x z} R_{y z}}{\left(\sum R_{x y}\right)^{2}} \\
& R_{y} R_{z}=\frac{R_{y z}^{2} R_{y x} R_{z x}}{\left(\sum R_{x y}\right)^{2}} \\
& R_{z} R_{x}=\frac{R_{z x}^{2} R_{y x} R_{y z}}{\left(\sum R_{x y}\right)^{2}}
\end{aligned}
$$

$R_{x} R_{y}+R_{y} R_{z}+R_{z} R_{x}=\frac{R_{x y} R_{y z} R_{z x}\left(R_{x y}+R_{y z}+R_{z x}\right)}{\left(\sum R_{x y}\right)^{2}}$

$$
\begin{gather*}
R_{x} R_{y}+R_{y} R_{z}+R_{z} R_{x}=\frac{R_{x y} R_{y z} R_{z x}\left(R_{x y}+R_{y z}+R_{z x}\right)}{\left(\sum R_{x y}\right)^{2}} \\
R_{x} R_{y}+R_{y} R_{z}+R_{z} R_{x}=\frac{R_{x y} R_{y z}}{\sum R_{y z}} R_{z x}=R_{x} R_{y z} \\
R_{y z}=\frac{R_{x} R_{y}+R_{y} R_{z}+R_{z} R_{x}}{R_{x}} \\
R_{y z}=R_{y}+R_{z}+\frac{R_{y} R_{z}}{R_{x}}  \tag{8}\\
R_{x y}=R_{x}+R_{y}+\frac{R_{x} R_{y}}{R_{z}}  \tag{9}\\
R_{z x}=R_{z}+R_{x}+\frac{R_{z} R_{x}}{R_{y}} \tag{10}
\end{gather*}
$$

Q 1) 2020-Aug (2018 scheme ECE) 2020-Aug (2018 scheme EE) 2017-June Determine the Input resistance between PQ using star-delta transformation


Figure 2
Solution:
In the given circuit $6 \Omega, 6 \Omega$ and 18 connected between $\mathrm{A}, \mathrm{B}$ and C are in delta connection, convert this into star network. The details are as shown in Figure 3

$$
\begin{aligned}
R_{A} & =\frac{R_{A B} \times R_{A C}}{\sum R_{A B}} \\
R_{A} & =\frac{6 \times 18}{30}=3.6 \Omega \\
R_{B} & =\frac{6 \times 6}{30}=1.2 \Omega \\
R_{C} & =\frac{6 \times 18}{30}=3.6 \Omega
\end{aligned}
$$



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Figure 3
In the circuit $5 \Omega$ and $3.6 \Omega$ are in series, $6 \Omega$ and $1.2 \Omega$ are in series and $3.6 \Omega 18 \Omega$ and $6 \Omega$ are in series.


Figure 4
$7.2 \Omega 27.6 \Omega$ are in parallel, which is in series with $8.6 \Omega$. The net resistance is.

$$
\begin{aligned}
R_{P Q} & =8.6+\frac{7.2 \times 27.6}{7.2+27.6} \\
& =8.6+5.71 \\
& =14.31 \Omega
\end{aligned}
$$

Q 2) For the circuit shown in Figure shown in Figure 5 determine the equivalent resistance between any two terminals.
Solution:


Figure 5
Solution:
In the given $4,4,4$, and $\Omega$ are in star network, convert this star network to delta network

$$
\begin{aligned}
& R_{x y}=R_{x}+R_{y}+\frac{R_{x} \times R_{y}}{R_{z}}=8+4=12 \Omega \\
& R_{x y}=4+4+\frac{4 \times 4}{4}=8+4=12 \Omega \\
& R_{y z}=4+4+\frac{4 \times 4}{4}=8+4=12 \Omega \\
& R_{z x}=4+4+\frac{4 \times 4}{4}=8+4=12 \Omega
\end{aligned}
$$

As shown in the Figure 6, by looking by any two terminals $12 \Omega$ is parallel with $4 \Omega$

$$
=\frac{12 \times 4}{12+4}=3 \Omega
$$



Figure 6
By looking from XZ terminal the $3 \Omega$ resistance is in parallel with series connection of $3 \Omega$ and $3 \Omega$ resistance.

$$
R_{X Z}=\frac{3 \times 6}{3+6}=2 \Omega
$$

Q 3) For the circuit shown in Figure shown in Figure 7 determine the equivalent resistance between (1)A and B and (2) A and N .


Figure 7
Solution:
Convert the internal star network to delta
network

$$
\begin{aligned}
& R_{A B}=R_{A}+R_{B}+\frac{R_{A} R_{B}}{R_{C}} \\
& R_{A B}=2+30+\frac{2 \times 30}{4}=32+15=47 \Omega \\
& R_{B C}=4+30+\frac{4 \times 30}{2}=34+60=94 \Omega \\
& R_{C A}=4+2+\frac{4 \times 2}{30}=6+0.266=6.266 \Omega
\end{aligned}
$$



Figure 8
In the circuit $10 \Omega$ is parallel with $47 \Omega$

$$
=\frac{10 \times 47}{10+47}=8.245 \Omega
$$

Similarly $94 \Omega$ is parallel with $15 \Omega$

$$
=\frac{94 \times 15}{94+15}=12.93 \Omega
$$

Similarly $6 \Omega$ is parallel with $6.266 \Omega$

$$
=\frac{6 \times 6.266}{6+6.266}=3.06 \Omega
$$

The details are as shown in Figure ??


Figure 9
While looking from terminal AB the resistances 12.93 and $\Omega$ and $3.06 \Omega$ are in series and this resistance is parallel with $8.245 \Omega$

$$
\begin{gathered}
=12.93+3.06=16 \Omega \\
R_{A B}=\frac{8.245 \times 16}{8.245+16}=5.44 \Omega
\end{gathered}
$$

(ii) The resistance between A and N is


Figure 10
From the Figure 10 by looking from the terminal resistance between A and N , there is a delta network between NCB which is replaced by star network.

$$
\begin{aligned}
R_{x} & =\frac{R_{x y} R_{x z}}{R_{x y}+R_{y z}+R_{z x}} \\
R_{B} & =\frac{30 \times 15}{30+15+4}=9.18 \\
R_{C} & =\frac{4 \times 15}{30+15+4}=1.225 \\
R_{N} & =\frac{30 \times 4}{30+15+4}=2.5
\end{aligned}
$$



Figure 11
In the network of $6 \Omega$ and $1.225 \Omega$ are in series, $10 \Omega$ and $9.18 \Omega$ are in series. The details are as shown in Figure 12


Figure 12


Figure 13
The resistances $7.225 \Omega$ and $19.18 \Omega$ are in
parallel

$$
=\frac{7.225 \times 19.18}{7.225 \times 19.18}=5.25 \Omega
$$

The details are as shown in Figure 14


Figure 14
The resistances $2.5 \Omega$ and $5.25 \Omega$ are in series. The resistances $2 \Omega 7.75 \Omega$ are in in parallel and the net resistance between A and N is

$$
=\frac{2 \times 7.75}{2+7.75}=1.59 \Omega
$$

Q 4) Determine the equivalent resistance between terminals A and B


Figure 15
Solution:

$$
\begin{aligned}
R_{A} & =\frac{4 \times 6}{20}=1.2 \Omega \\
R_{B} & =\frac{4 \times 10}{20}=2 \Omega \\
R_{C} & =\frac{6 \times 10}{20}=3 \Omega
\end{aligned}
$$

$$
R_{A}=\frac{10 \times 15}{45}=3.33 \Omega
$$

$$
R_{B}=\frac{10 \times 20}{45}=4.44 \Omega
$$

$$
R_{C}=\frac{20 \times 15}{45}=6.667 \Omega
$$



Figure 16


Figure 17

$$
\begin{aligned}
R_{A B} & =1.2+\frac{12.44 \times 18.667}{12.44+18.667}+3.3 \Omega \\
& =1.2+\frac{232.217}{12.44+31.187}+3.3 \Omega \\
& =1.2+7.446+3.3=11.94 \Omega
\end{aligned}
$$

Q 5) 2018-Dec (2010 scheme) Find the resistance of the circuit shown in Figure shown in Figure 5 between A and B


Figure 18
Solution:
In the given network 18 there is delta network between xyz and it is replaced by star network.

$$
\begin{aligned}
R_{X} & =\frac{20 \times 5}{40}=2.5 \Omega \\
R_{Y} & =\frac{20 \times 15}{40}=7.5 \Omega \\
R_{Z} & =\frac{15 \times 5}{40}=1.875 \Omega
\end{aligned}
$$



Figure 19
In the circuit $19,10 \Omega 2.5 \Omega$ are in series, similarly $5 \Omega 7.5 \Omega$ are in series. The details are as shown in Figure 20


Figure 20

In the circuit 20 at NPB $37.5 \Omega 3.875 \Omega$ and 30 are in delta connection, convert into star network. The details are as shown in Figure 21


Figure 21
In the circuit $21,12.5 \Omega, 2.045 \Omega$ are in series, similarly $1.635 \Omega 15 \Omega$ are in series. The details are as shown in Figure 22


Figure 22
In the circuit $2214.54 \Omega, 16.63 \Omega$ are in parallel, which is in series with similarly $15.76 \Omega$. The net resistance between AB is.

$$
\begin{aligned}
R_{A B} & =15.76+\frac{14.54 \times 16.63}{14.54+16.63} \\
& =15.76+7.76 \\
& =23.52 \Omega
\end{aligned}
$$

Q 6) For the circuit shown in Figure shown in Figure 5 determine the current i using star delta transformation.

Solution:


Figure 23
As shown in Figure 23 there is delta network between ABC , convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{1 \times 1}{1+1+1}=0.333 \Omega \\
R_{B} & =\frac{1 \times 1}{1+1+1}=0.333 \Omega \\
R_{C} & =\frac{1 \times 1}{1+1+1}=0.333 \Omega
\end{aligned}
$$



Figure 24
The resistances $0.333 \Omega$ and $2 \Omega$ are in series and $0.333 \Omega$ and $1 \Omega$ are in series.

The resistances $2.333 \Omega$ and $1.333 \Omega$ are in parallel its equivalent resistance is


Figure 25

$$
=\frac{2.333 \times 1.333}{2.333+1.333}=\frac{3.109}{3.666}=0.848 \Omega
$$

Total network resistance is $1+0.333+0.848=2.181 \Omega$

$$
I=\frac{1}{2.181}=0.458 A
$$

Q 7) Calculate the current in the $40 \Omega$ resistance of the circuit shown in Figure shown in Figure 5 using star delta transformation.


## Figure 26

Solution:
As shown in Figure 23 there is delta network between ABC, convert this to star network

$$
\begin{aligned}
& R_{A}=\frac{20 \times 5}{30}=3.333 \Omega \\
& R_{B}=\frac{5 \times 5}{30}=0.833 \Omega \\
& R_{C}=\frac{20 \times 5}{30}=3.333 \Omega
\end{aligned}
$$



Figure 27


Figure 28
The total resistance of the network is

$$
\begin{aligned}
& =3.333+\frac{40.833 \times 3.333}{40.833+3.333}=3.333 \Omega \\
& =3.333+\frac{136}{44.163}=3.333+3.08+\Omega \\
& =6.41 \Omega
\end{aligned}
$$

The total current flowing in the network is

$$
I_{1}=\frac{4}{6.41}=0.624 A
$$

Using branch current division method the current in $40 \Omega$ is

$$
I_{3}=0.624 A \frac{3.333}{44.163}=0.047 A
$$

Q 8) Determine the currents supplied by the each battery using star-delta transformation


Figure 29
Solution:
As shown in Figure 29 there is delta network between ABC, convert this to star network

$$
\begin{aligned}
& R_{A}=\frac{4 \times 6}{15}=1.6 \Omega \\
& R_{B}=\frac{4 \times 5}{15}=1.3 \Omega \\
& R_{C}=\frac{6 \times 5}{15}=2 \Omega
\end{aligned}
$$



Figure 30
In the circuit $30,3 \Omega$ and $1.6 \Omega$ are in series and also $2 \Omega$ and $1.3 \Omega$ are in series. The details are as shown in Figure 31


Figure 31


Figure 32

$$
I_{3}=I_{1}+I_{2}
$$

KVL for loop 1

$$
\begin{aligned}
15-4.6 I_{1}-2 I_{3} & =0 \\
15-4.6 I_{1}-2 I_{1}-2 I_{2} & =0 \\
15-6.6 I_{1}-2 I_{2} & =0 \\
6.6 I_{1}+2 I_{2} & =15
\end{aligned}
$$

KVL for loop 2

$$
\begin{aligned}
20-3.3 I_{2}-2 I_{3} & =0 \\
20-3.3 I_{2}-2 I_{1}-2 I_{2} & =0 \\
20-5.3 I_{2}-2 I_{1} & =0 \\
2 I_{1}+5.3 I_{2} & =20
\end{aligned}
$$

Simultaneous equations are

Figure 33
Solution:


Figure 34

$24.3 \Omega$
Figure 35

$$
\begin{aligned}
R_{A B} & =1.87+\frac{6.94 \times 3.55}{6.94 \times 3.55} \\
& =38+24.3+80=142.3 \Omega
\end{aligned}
$$

### 0.2 Question Papers

## Question Papers

2019-Jan (2017 scheme ECE) Find the equivalent resistance between a and b as shown in Figure 36 using star delta transformation


Figure 36: JAN-2019-Question Paper
Solution:
As shown in Figure 36 there is delta network between $8 \Omega 5 \Omega$ and $4 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{8 \times 5}{8+4+5}=2.35 \Omega \\
R_{B} & =\frac{5 \times 4}{17}=1.17 \Omega \\
R_{C} & =\frac{8 \times 4}{17}=1.88 \Omega
\end{aligned}
$$



Figure 37


Figure 38
As shown in Figure 38 there is delta network between $6 \Omega 5.17 \Omega$ and $5.35 \Omega$, convert this to star
network

$$
\begin{aligned}
R_{A} & =\frac{6 \times 5.17}{6+5.17+5.35}=1.87 \Omega \\
R_{B} & =\frac{5.17 \times 5.35}{16.52}=1.67 \Omega \\
R_{C} & =\frac{6 \times 5.35}{16.52}=1.94 \Omega
\end{aligned}
$$



Figure 39


Figure 40

$$
\begin{aligned}
R_{A B} & =1.87+\frac{6.94 \times 3.55}{6.94 \times 3.55} \\
& =1.87+2.34=4.21 \Omega
\end{aligned}
$$

2019-DEC Determine the resistance between A and B of the network shown in Figure 41.


Figure 41: 2019-DEC
Solution:


Figure 42
As shown in Figure 42 there is delta network between $2 \Omega 3 \Omega$ and $6 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{10 \times 30}{10+10+30}=6 \Omega \\
R_{B} & =\frac{10 \times 30}{50}=6 \Omega \\
R_{C} & =\frac{10 \times 10}{50}=2
\end{aligned}
$$



Figure 43


Figure 44
As shown in Figure 44 there is delta network between $6 \Omega 12.5 \Omega$ and $24.5 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{6 \times 12.5}{6+12.5+24.5}=1.74 \Omega \\
R_{B} & =\frac{6 \times 24.5}{43}=3.41 \Omega \\
R_{C} & =\frac{12.5 \times 24.5}{43}=7.12 \Omega
\end{aligned}
$$



Figure 45


Figure 46

$$
\begin{aligned}
R_{A B} & =1.74+\frac{9.41 \times 19.62}{9.41 \times 19.62}=1.74+6.36 \\
& =8.1 \Omega
\end{aligned}
$$

Also by observation its a wheatstone bridge because the ratio is

$$
\frac{12.5}{12.5}=\frac{6}{6}=1
$$

Hence no current flows between E D

$$
R_{A B}=\frac{25 \times 12}{25 \times 12}=8.1 \Omega
$$

2019-DEC Determine the resistance between A and B of the network shown in Figure 41.


Figure 47: 2019-June-(2015-scheme-ECE)1
Solution:


Figure 48
As shown in Figure 48 there is star network between $2 \Omega 3 \Omega$ and $5 \Omega$, convert this to star network

$$
\begin{aligned}
& R_{A B}=2+3+\frac{2 \times 3}{5}=5+1.2=6.2 \Omega \\
& R_{A E}=2+5+\frac{2 \times 5}{3}=7+3.3=10.3 \Omega \\
& R_{B E}=5+3+\frac{5 \times 3}{2}=8+7.5=15.5 \Omega
\end{aligned}
$$



Figure 49

$$
=\frac{10 \times 15.5}{10 \times 15.5}=6.07 \Omega
$$



Figure 50
As shown in Figure 50 there is a delta network between $6.2 \Omega 10.33 \Omega$ and $6.07 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{6.2 \times 10.33}{6.2+10.33+6.07}=2.83 \Omega \\
R_{B} & =\frac{6.2 \times 6.07}{22.6}=1.67 \Omega \\
R_{E} & =\frac{6.07 \times 10.33}{22.6}=2.77 \Omega
\end{aligned}
$$



Figure 51


Figure 52
As shown in Figure 52 there is a delta network between $2.83 \Omega 6 \Omega$ and $10.77 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{2.83 \times 6}{19.6}=0.87 \Omega \\
R_{E} & =\frac{2.83 \times 10.77}{19.6}=1.55 \\
R_{D} & =\frac{10.77 \times 6}{19.6}=3.3
\end{aligned}
$$



Figure 53


Figure 54
$=0.87+\frac{3.22 \times 7.3}{3.22+7.3}=0.87+2.23$
$=3.1 \Omega$

2018-Dec,2014-Dec Using star/delta transformation determine the resistance between M and N of the network shown in Figure 55.


Figure 55: 2018-DEC-(2015-scheme-ECE)1
Solution:


Figure 56
As shown in Figure 56 there is delta network between $2 \Omega 3 \Omega$ and $6 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{2 \times 3}{2+3+6}=0.545 \Omega \\
R_{B} & =\frac{3 \times 6}{11}=1.636 \Omega \\
R_{C} & =\frac{6 \times 2}{11}=1.1 \Omega
\end{aligned}
$$



Figure 57


Figure 58
As shown in Figure 59 there is delta network between $1.1 \Omega 5.636 \Omega$ and $5 \Omega$, convert this to star
network


Figure 59


Figure 60
$R_{B}=\frac{1.195 \times 9.43}{1.195+9.43}=1.06 \Omega$

$$
R_{M N}=1+1.06+0.468=2.528 \Omega
$$

2015-Dec Find the equivalent resistance between A and B of the network shown in Figure 61 using StarDelta transformation.


Figure 61: 2015-DEC
Solution:


Figure 62
As shown in Figure 62 there is delta network between $15 \Omega 8 \Omega$ and $5 \Omega$, and there is delta network
between $9 \Omega 9 \Omega$ and $9 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{15 \times 8}{28}=4.28 \Omega \\
R_{D} & =\frac{5 \times 8}{28}=1.42 \Omega \\
R_{C} & =\frac{15 \times 5}{28}=2.67 \Omega \\
R_{B} & =\frac{9 \times 9}{27}=3 \Omega \\
R_{E} & =\frac{9 \times 9}{27}=3 \Omega \\
R_{F} & =\frac{9 \times 9}{27}=3 \Omega
\end{aligned}
$$



Figure 63



Figure 64
15.67 and $14.42 \Omega$ are in parallel

$$
\begin{aligned}
& =\frac{15.67 \times 14.42}{15.67 \times 14.42}=7.51 \Omega \\
R_{A B} & =4.28+7.51+3=14.79 \Omega
\end{aligned}
$$



Figure 66: 2013-DEC1


Figure 67: 2013-DEC1


Figure 68: 2013-DEC1


Figure 69: 2013-DEC1

2013-DEC1 Using star/delta transformation determine the resistance between M and N of the network shown in Figure 65.


Figure 65: 2013-DEC1

2008-June Using star/delta transformation determine the resistance between M and N of the network shown in Figure 70.


Figure 70: 2008-June

Solution:
Solution:


Figure 71: 2008-June
As shown in Figure 71 there is delta network between A C D $5 \Omega 5 \Omega$ and $10 \Omega$, and there is delta network between $\mathrm{B} \mathrm{C} \mathrm{E} 5 \Omega 5 \Omega$ and $10 \Omega$, convert this to star network

$$
\begin{aligned}
R_{A} & =\frac{5 \times 5}{20}=1.25 \Omega \\
R_{C} & =\frac{5 \times 10}{20}=2.5 \Omega \\
R_{D} & =\frac{5 \times 10}{20}=2.5 \Omega \\
R_{B} & =\frac{5 \times 5}{20}=1.25 \Omega \\
R_{E} & =\frac{5 \times 10}{20}=2.5 \Omega \\
R_{F} & =\frac{5 \times 10}{20}=2.5 \Omega
\end{aligned}
$$



Figure 72: 2008-June22


Figure 73: 2008-June23


Figure 74: 2008-June24

$$
\begin{aligned}
R_{A B} & =1.25+3.33+1.25 \\
& =5.83 \Omega
\end{aligned}
$$

2007-July Using star/delta transformation determine the resistance between A and B of the network shown in Figure 75.


Figure 75: 2007-July
Solution:
As shown in Figure 75 there is star network between $6 \Omega 6 \Omega$ and $6 \Omega$, convert this to star to delta network

$$
\begin{aligned}
& R_{A B}=6+6+\frac{6 \times 6}{6}=12+6=18 \Omega \\
& R_{A C}=6+6+\frac{6 \times 6}{6}=12+6=18 \Omega \\
& R_{B C}=6+6+\frac{6 \times 6}{6}=12+6=18 \Omega
\end{aligned}
$$

Figure 76: 2007-July
$18 \Omega$ between AC and AB are in parallel

$$
=\frac{18 \times 18}{36}=9 \Omega
$$



Figure 77: 2007-July
$9 \Omega$ and $9 \Omega$ are in series which is in parallel with $18 \Omega$

$$
A B=18+\frac{9 \times 9}{18}=18+4.5=22.5 \Omega
$$

Using star/delta transformation determine the resistance between A and B of the network shown in Figure 78.


Figure 78
Solution:



Figure 79


Figure 80


Figure 81
$R_{P Q}=7+7.785+2=16.785 k \Omega$

